## MATHEMATICS

## TIME: $\mathbf{2}^{1 ⁄ 2} \mathbf{2}$ HOURS

## NAME

$\qquad$ ADM NO: $\qquad$

SIGN
DATE;

## INSTRUCTIONS TO STUDENTS

1. Answer all questions in this question paper.
2. All your answers must be written in the spaces provided in this question paper.
3. Evaluate without using tables or calculators.

$$
\frac{0.036 \times 0.0049}{0.07 \times 0.048}
$$

2. The sum of interior angles of a regular polygon. Find the size of each exterior angle. (3mks)
3. The length of an arc of a circle is $\overline{5}$ of its circumference. If the area of the circle is $346.5 \mathrm{~cm}^{2}$, find the angle subtended by the arc at the Centre of the circle.
4. Given that $x=2 y$ and $3 y=5 z$. find the ratio $x: y: z$ hence or otherwise find the amount of money Ali got if Ali, Ben and Chris shared Kshs. 36000 in the ratio x:y:z respectively. (4mks)
5. A plane leaves town A for town B at 0540 hours. If the journey takes 6.5 hours, at what time does the plane reach its destination?
6. A cylindrical solid metal is 3 m long and has a mass of 4 kg . if its density is $5.6 \mathrm{~g} / \mathrm{cm}^{3}$, find the radius of its end. (take $\pi=3.142$ )
7. Express the number 9000 as a product of its prime factors.
b) Find the value of P if the number 9000 P is a perfect cube.
8. Find the value of T given that $\mathrm{T}=\frac{a b}{a^{3}+b c}$ and $\mathrm{a}=2, \mathrm{~b}=-1$, and $\mathrm{c}=-3$ (3mks)
9. A shop keeper sells a shirt for Kshs. 350 thereby making a profit of $40 \%$. Calculate the buying price of the shirt.
10. The GCD of three numbers is 45 and their LCM is 18900 . Two of the numbers are 675 and 540. Find the other possible numbers.
11. Find the perimeter of the figure below. (Take $\pi=22 / 7$ ).

12. John is twice as old as his friend Peter. Peter is 5 years older than Alice. In 5 years John will be three times as old as Alice. How old is Peter now?
13. Ondieki had travelled from Texas to Kenya and arrived with U\$17500 on 12/2/2013. On arrival he changed the dollars into Kenya shillings and immediately used Kshs. 850,000. Later on $15 / 2 / 2013$ he had some immediate use of $£ 3600$ and therefore $c$ hanged all the money he had into sterling pounds. Finally on $18 / 2 / 2013$ he converted what remained to Kenya shillings.

## Buying

Selling
Kshs.Kshs.
12/2/2013 U\$ 82.36
85.74

15/2/2013 £ 110.14
118.26

18/2/2013£ 112.64
119.56

How much did he remain with in Kenya shillings?
(3mks)
14. The sum of the digits of a two digits number is 13 . If the digits are reversed the number decrease by 27 . Find the number.
15. A man walks to work at $16 \mathrm{~km} / \mathrm{hr}$ and back home at $5 \mathrm{~km} / \mathrm{hr}$. find the distance from his work place if the whole journey takes him 2 hours 12 minutes.
16. If $3=-\frac{1}{\mathbf{4} x}=\frac{\mathbf{1}}{\mathbf{8 x}}$, find the ratio $\frac{\mathbf{1}}{\mathbf{2 x}}+2: \frac{\mathbf{1}}{\mathbf{3 x}}+\mathbf{1}$

## SECTION II (50 MARKS) ANSWER ANY FIVE QUESTIONS

17. (a) Using a ruler and a pair of compasses only construct a triangle $A B C$ such that $A B=4 \mathrm{~cm}$, $\mathrm{BC}=5 \mathrm{~cm}$ and $\angle \mathrm{ABC}=120^{\circ}$. Measure AC .
b) On the diagram, construct a circle which passes through the vertices of the triangle $A B C$. Measure the shortest distance from the centre of the circle to line BC.
c) Measure the radius of the circle.
18. Two aero planes $P$ and $Q$ leave an airport at the same time. $P$ flies on a bearing of $240^{\circ}$ at $900 \mathrm{~km} / \mathrm{h}$ while Q flies due East at $750 \mathrm{~km} / \mathrm{h}$.
a) Using a scale drawing of 1 cm to represent 100 km , make a scale drawing to show the positions of the planes after 40 minutes.
b) Determine the bearing of
i) $P$ from $Q$
ii) $Q$ from $P$
c) Find the shortest distance between plane P and plane Q after 40 minutes. ( 1 mk )
19. A construction company requires to transport 144 tonnes of stones to sites A and B. the company pays Kshs. 24000 to transport 48 tonnes of stone for every 28 km . kimani transported 96 tonnes to a site A, 49 km away.
a) Find how much he paid. (3mks)
b) Kimani spends Kshs. 3000 to transport every 8 stones to the site. Calculate his total profit. (4mks)
c) Achieng transported the remaining stones to sites B, 84 km away. If she made $44 \%$ profit, find her transport cost.
(3mks)
20. A tank has two inlet taps $P$ and $Q$ and an outlet tap $R$. when empty, the tank can be filled by $\operatorname{tap} \mathrm{P}$ in $4^{1} / 2$ hours and by tap Q in 3 hours. When full the tap can be emptied in 2 hours by tap R.
a) The tank is initially empty, find how long it would take to fill up the tank;
i) If $\operatorname{tap} \mathrm{R}$ is closed and taps P and Q are opened at the same time.
ii) If all the three taps are opened at the same time.
b) Find the fraction of the tank that would be filled by 9.00am if initially the tank is empty and the taps are opened as follows.
(4mks)
P at $\quad 8.00 \mathrm{am} \quad \mathrm{R}$ at 9.00 am
Q at 8.45 am
21. a) Plot the graphs of the equations $y=2 x+3$ and $y=-1 / 2 x+3$. (4mks)

b) Use your graph to find the coordinates of the point of intersection of the two lines. (2mks)
c) Hence, state the solutions to the equations $y=2 x+3$ and $y=-1 / 2 x+3 . \quad(2 \mathrm{mks})$
d) Find the angle made by the line $y=2 x+3$ and the $x$-axis.
22. A coffee farm was surveyed and its measurements entered in a field book as shown below. (Take XY $=400 \mathrm{~m}$ as the baseline.)

|  |  | Y |
| :--- | :--- | :--- |
| $360 \quad 80$ to Q |  |  |
| to $\mathrm{R} 80 \quad 280$ |  |  |
| to $\mathrm{S} 160 \quad 200$ |  |  |
| $40 \quad 200$ to P | X |  |

a) Using a scale of 1 cm to represent 40 m , draw the map of the coffee farm. (3mks)
b) Find the area of the coffee farm in hectares.
23. A model of a tent consists of cube and a pyramid on a square base as shown below.

a) Draw accurately the net of the model.
(2mks)
b) Use the net to calculate the total surface area of the model. ( 4 mks )
c) If the ratio of the area of the model to the area of the actual is $1: 10000$, find the area of the material required to make the tent (floor area inclusive) in $\mathrm{m}^{2}$.
24. a) Water and alcohol are mixed in the ratio $1: 4$. Find the density of the mixture if the density of water is $1 \mathrm{~g} / \mathrm{cm}^{3}$ and that of alcohol is $0.8 \mathrm{~g} / \mathrm{cm}^{3}$.
b) $40 \mathrm{~cm}^{3}$ of water is poured into an empty measuring cylinder. A stone of mass 129 g is put into the cylinder. If the density of the mixture of the stone is $8.6 \mathrm{~g} / \mathrm{cm}^{3}$, find the new reading of the cylinder.
c) Convert $8.6 \mathrm{~g} / \mathrm{cm}^{3}$ into $\mathrm{kg} / \mathrm{m}^{3}$.
(2mks)

