# END OF TERM 1 EXAMS 

## MATHEMATICS

 FORM THREE PAPER 2TIME: $21 ⁄ 2$ HOURS

NAME. .ADM NO:...........................

SIGN.......................................................................... INDEX NO: $\qquad$

SECTION A (50MARKS)
Answer all questions in this section in the spaces provided.

1. Evaluate:

$$
3 / 8 \text { of }\left\{7 \frac{3}{5}-1 / 3(11 / 4+31 / 3) \times 2 \frac{2}{5}\right\}
$$

2. Solve the simultaneous equations

$$
\begin{aligned}
& x y=4 \\
& x+y=5
\end{aligned}
$$

3. A man invests Ksh.24, 000 in an account which pays $16 \%$ interest p.a. the interest is compounded quarterly. Find the amount in the account after $11 / 2$ years.
4. Given that position vectors of points A and B are $\underset{\sim}{\mathrm{a}}=\binom{-3}{2}$ and $\underset{\sim}{\mathrm{b}}=\binom{2}{5}$ and C is a point on AB such that $\mathrm{AC}: \mathrm{CB}=1: 2$. Find the coordinates of the point C .
5. The table below shows the number of goals scored in 40 soccer matches during a certain season.

| No. of goals | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| No. of matches | 3 | 9 | 6 | 8 | 5 | 5 | 2 | 1 |

6. Simplify:

$$
\frac{\chi^{2}-\chi y}{(\chi+y)^{2}} \div \frac{(\chi-y)^{2}}{\chi^{2} y-y^{3}}
$$

7. From a point 20 m away on a level ground the angle of elevation to the lower window line is $25^{\circ}$ and the angle of elevation to the top line of the window is $34^{\circ}$. Calculate the height of the window. (3mks)
8. Find the distance round the figure given below. (Take $\Pi=\frac{22}{7}$ ) (2mks)

9. Find all the integral values of $\chi$ which satisfy the inequalities.

$$
\chi+8>4 \chi-6 \geq 3(4-\chi)
$$

10. Agnes paid rent which was $1 / 10$ of her net salary. She used $1 / 2$ of the remaining amount to make a down payment for a plot. She gave her mother Kshs. 2,500 and did shopping worth Kshs. 7,500 for herself. She saved the remainder which was Ksh. 12,500 . How much was the down payment that she made. (4mks)
11. The figure below is a velocity time graph for a car.

12. A chord $\mathbf{P Q}$ of length 15 cm subtends an angle of $65^{\circ}$ at the circumference centre $\mathbf{O}$. Find the radius of the circle.
13. The interior angles of a hexagon are $2 x+5,4 x-5,4 x+5,3 x, 4 x-20$ and $2 x$.

Find the value of $\mathbf{x}$.
(3mks)
14. A line passes through the point $(-1,2)$ and has gradient $-1 / 2$. Write down its equation in the form $\boldsymbol{a} \boldsymbol{x}+\boldsymbol{b} \boldsymbol{y}=$ c (3mks)
15. Given $\mathrm{x}=13.4 \mathrm{~cm}$ and $\mathrm{y}=4.3 \mathrm{~cm}$. calculate the percentage error in $\frac{X}{Y}$ correct to 4 d.p (4mks)
16. The figure below is a cone whose base radius is 3.5 cm and slant height 7 cm . The net of the cone is a sector of a circle.

(a) Find the angle subtended at the centre of the sector.
(2mks)
(b) Draw the net of the solid.
(1mk)

Answer any five questions from this section in the spaces provided.
17. A straight line $L_{1}$ has a gradient $-1 / 2$ and passes through point $P(-1,3)$. Another line $L_{2}$ passes through the points $\mathrm{Q}(1,-3)$ and $\mathrm{R}(4,5)$. Find.
(a) The equation of $L_{1}$.
(2mks)
(b) The gradient of $L_{2}$.
(1mk)
(c) The equation of $\mathrm{L}_{2}$.
(2mks)
(d) The equation of a line passing through a point $S(0,5)$ and is perpendicular to $L_{2}$. ( 3 mks )
(e) The equation of a line through R parallel to $\mathrm{L}_{1}$.
(a) Given that $\mathrm{y}=7+3 \chi-\chi^{2}$, complete the table below.

| $\chi$ | -3 | -2 | -1 | 0 | 1 | 2 | 3 | 4 | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| y | -11 |  |  | 7 |  |  |  |  |  | -11 |

(b) On the grid provided and using a suitable scale draw the graph of

$$
\begin{equation*}
y=7+3 \chi-\chi^{2} \tag{2mks}
\end{equation*}
$$

(c) On the same grid draw the straight line and use your graph to solve the equation $\chi^{2}-4 \chi-3=0$.
(3mks)
(d) Determine the coordinates of the turning point of the curve.
(2mks)
19. From a reservoir, water flows through a cylindrical pipe of diameter 0.2 m at a rate of 0.35 m per second.
(a) Determine the number of liters of water discharged from reservoir in one hour. (4mks)
(b) The water flows from the reservoir for 18 hours per day for 25 days per month and serves a population of 2500 families. Determine the average consumption of water per family per month giving your answer to the nearest 100 litres.
(4mks)
(c) The water is charged at the rate of sh. 4.50 per 100 litres. Calculate the average water bill per family per month.
(2mks)
20. In the figure below PQR is a tangent to the circle at Q . TS is a diameter and TSR and QUV are straight lines. QS is parallel to TV. Angles $\mathrm{SQR}=40^{\circ}$ and $\mathrm{TQV}=55^{\circ}$.

(a) Find the following angles giving reasons each case.
(i) <QTS
(2mks)
(ii) <QRS
(iii) <QVT

## (iv) <QUT

(b) Given that $\mathrm{QR}=8 \mathrm{~cm}$, and $\mathrm{SR}=4 \mathrm{~cm}$. Find the radius of the circle.
21. Mr. Kimutai a teacher from Tuiyotich Secondary School earns K£ 12000 per annum and lives in a house provided by the employer at a minimum rent of Ksh. 2000 per month. He gets a family relief of K£ 1320p.a. and is entitled to a relief of $10 \%$ of his insurance of $\mathrm{K} £ 800$ p.a.
(a) Calculate his annual tax bill based on the table below. (6mks)

| Income slab in K£ p.a. | $\frac{\text { Rate }}{10 \%}$ |
| :---: | :---: |
| $1-2100$ | $15 \%$ |
| $2101-4200$ | $25 \%$ |
| $4201-6300$ | $35 \%$ |
| $6301-8400$ | $45 \%$ |
| Over 8400 |  |

(b) Kimutai other deductions include.

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-W.C.P.S = sh 600.00pm
- NHIF = sh 500.00pm
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Calculate Kimutai's net salary monthly.
(4mks)
(a) 22. The diagram represents a solid frustum with base radius of 35 cm and top radius of 21 cm . The frustum is 22.5 cm high and is made of a metal whose density is $4 \mathrm{~g} / \mathrm{cm}^{3}$. Taking $\pi=22 / 7$,


Calculate;
(i) The volume of the metal that makes the frustum.
(6mks)
(b) The frustum is melted in down and recast into a solid cube in the process $20 \%$ of the metal is lost. Calculate to 2d.p the length of each side of the cube.
23. Four points $\mathbf{B}, \mathbf{C}, \mathbf{Q}$ and $\mathbf{D}$ lie on the same plane. Point $B$ is 42 km due southwest point $\mathbf{Q}$. Point $\mathbf{C}$ is 50 km on a bearing of $\mathrm{S} 60^{\circ} \mathrm{E}$ from $\mathbf{Q}$. Point $\mathbf{D}$ is equidistant from $\mathbf{B}, \mathbf{Q}$ and $\mathbf{C}$.
(a) Using the scale: 1 cm represents 10 km , construct a diagram showing the positions of $\mathbf{B}, \mathbf{C}, \mathbf{Q}$ and $\mathbf{D}$.
(5mks)
(b) Determine the
(i) Distance between $\mathbf{B}$ and $\mathbf{C}$
(1mk)
(c) Find the distance and bearing of $\mathbf{D}$ from $\mathbf{C}$.
(2mks)
24. (a) A small field was surveyed and the measurements recorded in a surveyor's field book as in the table below.

|  |  | 100 | 0 | F |
| :--- | :--- | :---: | :--- | :--- |
|  |  | 65 | 40 | D |
| $\mathbf{E}$ | 30 | 50 |  |  |
|  |  | 30 | 25 | B |
| $\mathbf{C}$ | 20 | 20 |  |  |
| $\mathbf{A}$ | 0 | 0 |  |  |

(i) Using a scale of 1 cm to 10 m make an accurate drawing of the map of the field. (4mks)
(ii) Find the area of the field.
(3mks)
(iii) Assuming that the baseline in (a) runs in a northern direction give the position of $\mathbf{D}$ relative to A using bearing and distance. (3mks)

